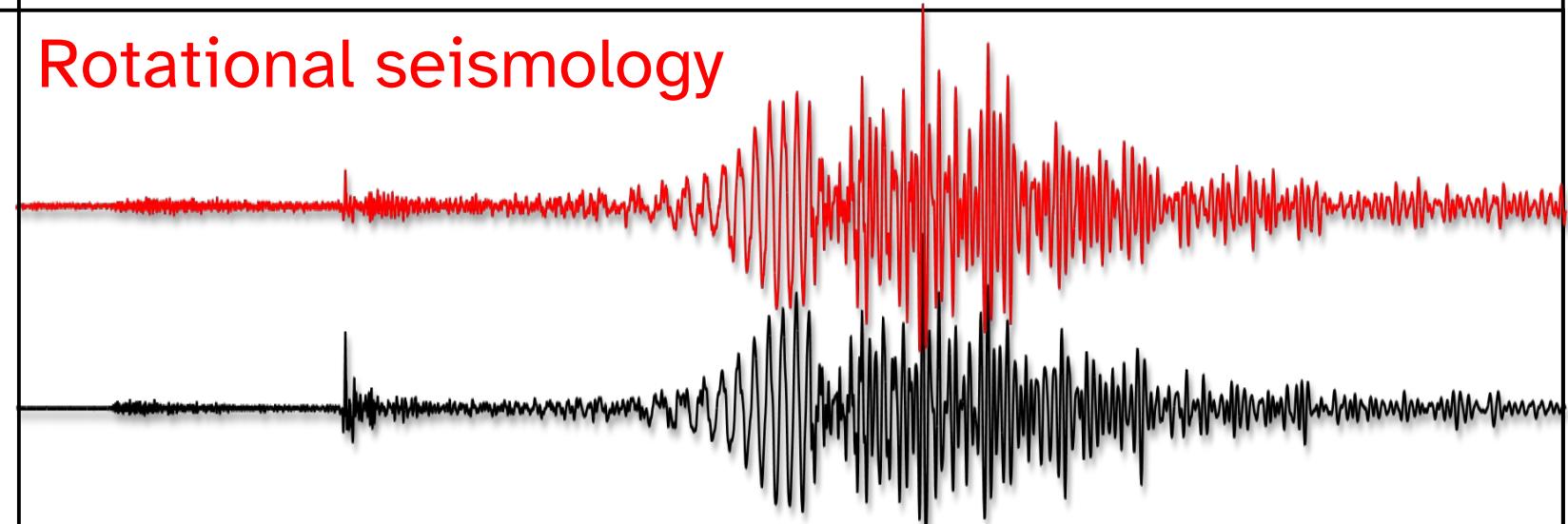


Rotational seismology



Céline Hadzioannou (and many others..)



University of Hamburg, Germany

Rotational seismology

Rotational rate

Transverse acceleration

Céline Hadzioannou (and many others..)

University of Hamburg, Germany

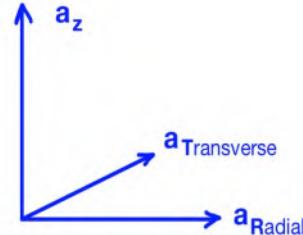


What are rotations?

Entire ground motion, all degrees of freedom

$$u(x+\delta x) = u(x) + \varepsilon \delta x + \omega \times \delta x$$

3C Translation



Ground acceleration
Seismometer



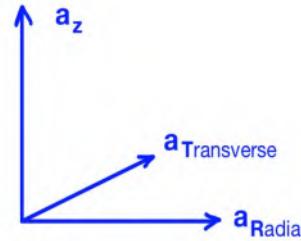
What are rotations?

Entire ground motion, all degrees of freedom

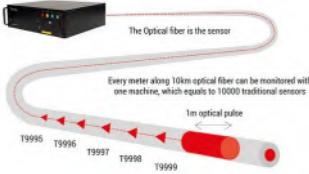
$$u(x+\delta x) = u(x) + \varepsilon \delta x + \omega \times \delta x$$

3C Translation

+ 6C Strain



Ground acceleration
Seismometer



Strain
Strainmeter,
Distributed
Acoustic
Sensing (DAS)

What are rotations?

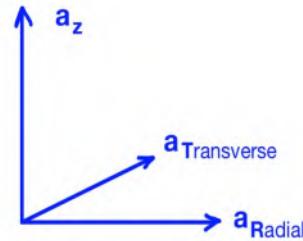
Entire ground motion, all degrees of freedom

$$u(x+\delta x) = u(x) + \varepsilon \delta x + \omega \times \delta x$$

3C Translation

+ 6C Strain

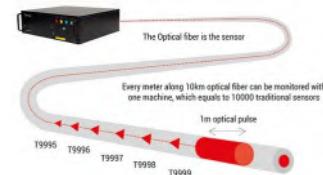
+ 3C Rotation



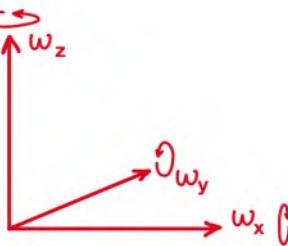
Ground acceleration
Seismometer



Strain
Strainmeter,
Distributed
Acoustic
Sensing (DAS)



Rotation rate
Rotation sensor



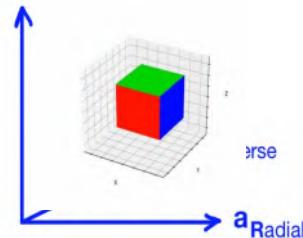
Review: e.g. Cochard et al.,
2006; Schmelzbach 2018

What are rotations?

Entire ground motion, all degrees of freedom

$$u(x+\delta x) = u(x) + \varepsilon \delta x + \omega \times \delta x$$

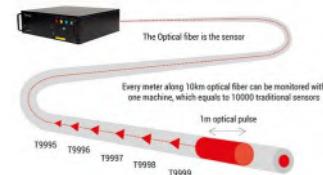
3C Translation



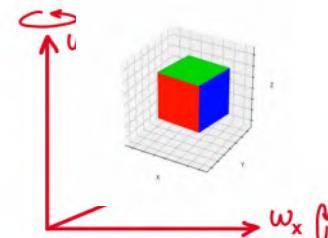
Ground acceleration
Seismometer



Strain
Strainmeter,
Distributed
Acoustic
Sensing (DAS)



+ 3C Rotation



Rotation rate
Rotation sensor



Animation by Felix Bernauer
Review: e.g. Cochard et al.,
2006; Schmelzbach 2018

Why?



Structural engineering

Why?



Source

Structure

Wavefield

Structural engineering

Why?



Source

Structure

Instrumentation

Wavefield

Structural engineering

Why?



Source

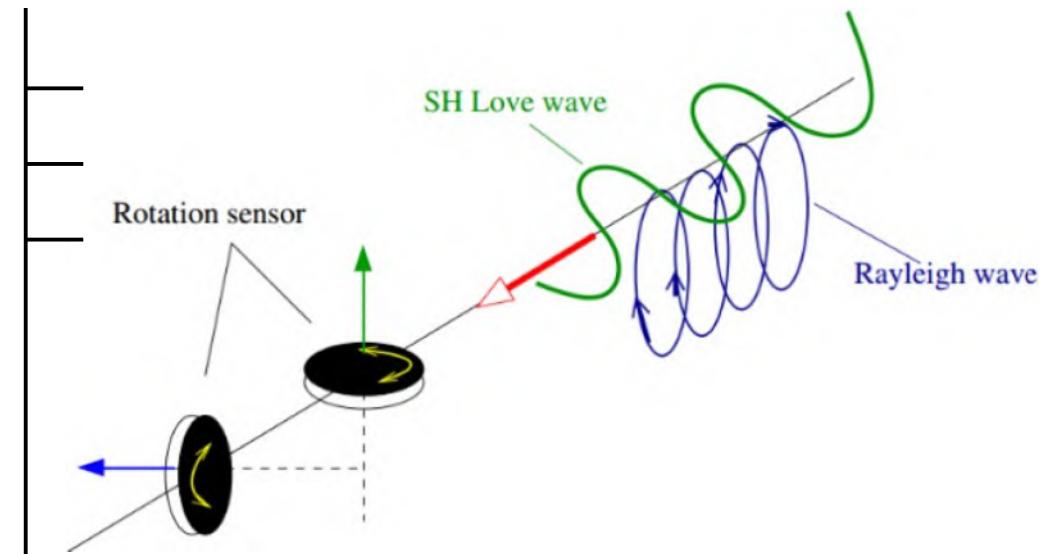
Structure

Instrumentation

Wavefield

Structural engineering

Rotations → wavetype filter

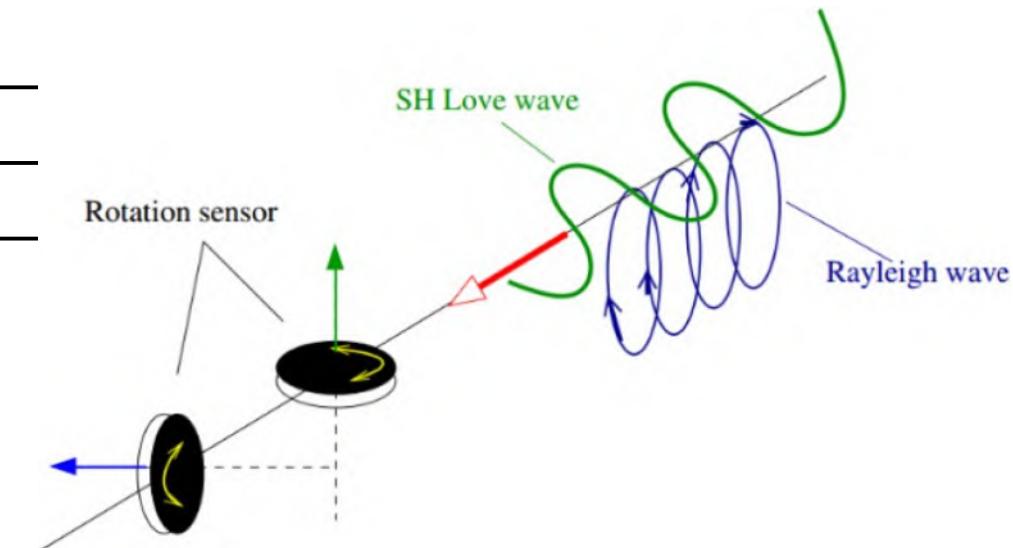
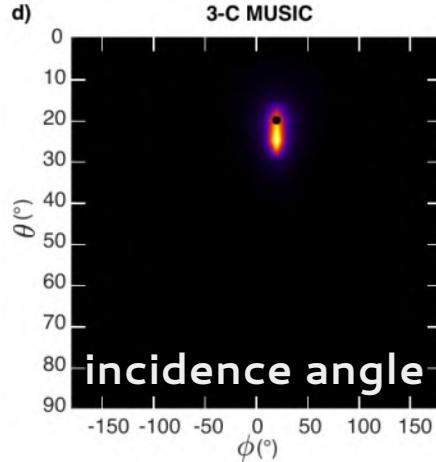
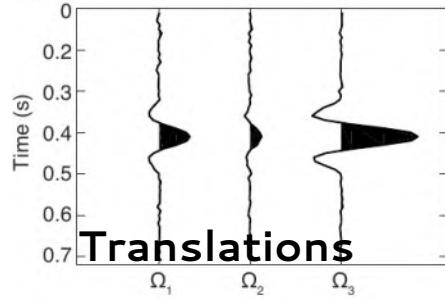


Love & SH motion → vertical rotation
Rayleigh → horizontal rotation

Rotations → wavetype filter

Polarization analysis: 3 vs 6 components

3-C MUSIC Result

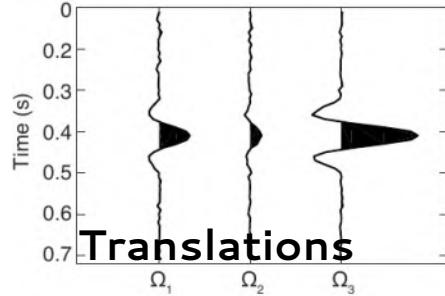


Love & SH motion → vertical rotation
Rayleigh → horizontal rotation

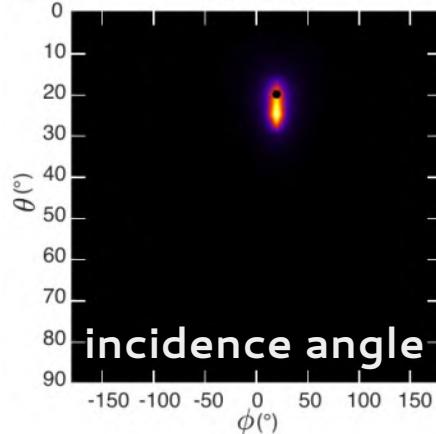
Rotations → wavetype filter

Polarization analysis: 3 vs 6 components

b) 3-C MUSIC Result

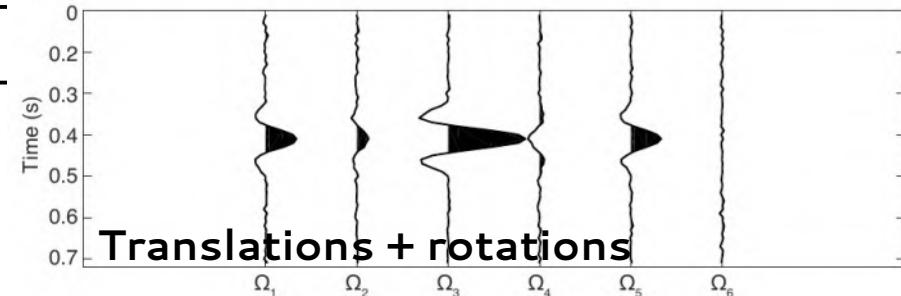


d) 3-C MUSIC

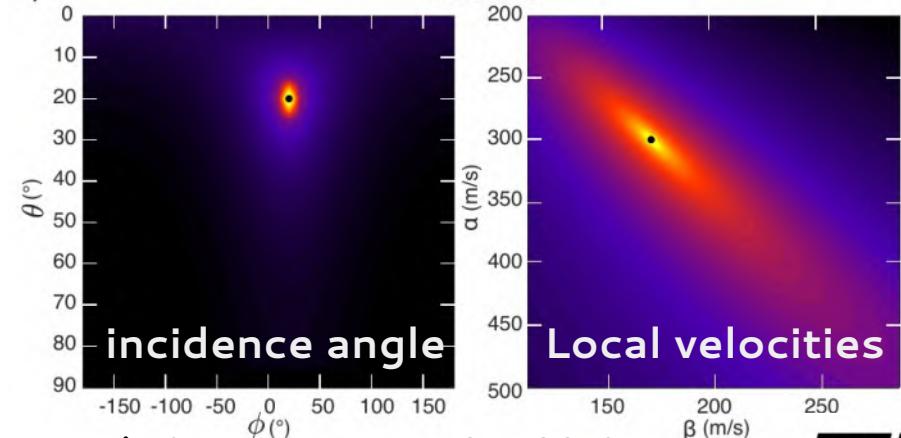


Sabrina Keil

a) 6-C MUSIC Result



c) 6-C MUSIC



David Sollberger et al. GJI 2018

ETH Zürich

Source

Structure

Instrumentation

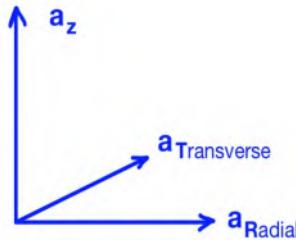
Wavefield

- Wavetype separation
- Wavetype ratios

Structural engineering

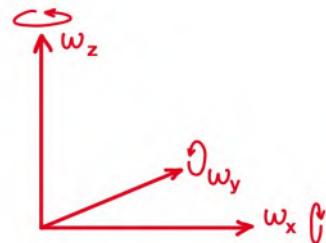
Combining Rotation and Translation

3C Translation



Ground acceleration
Seismometer

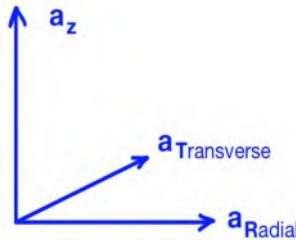
+ 3C Rotation



Rotation rate
Rotation sensor

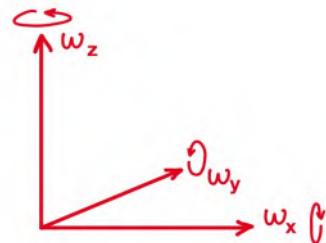
Combining Rotation and Translation

3C Translation



Ground acceleration
Seismometer

+ 3C Rotation

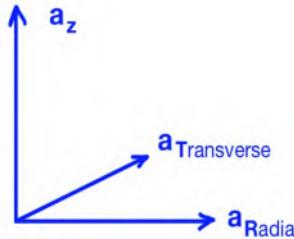


Rotation rate
Rotation sensor

$$\frac{a_T}{\dot{\omega}_z}$$

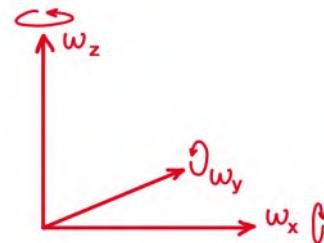
Combining Rotation and Translation

3C Translation



Ground acceleration
Seismometer

+ 3C Rotation

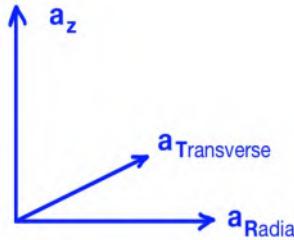


Rotation rate
Rotation sensor

$$\frac{a_T}{\dot{\omega}_z} = \frac{-k^2 c^2 A \sin(kx - kct)}{\frac{1}{2} k^2 c A \sin(kx - kct)}$$

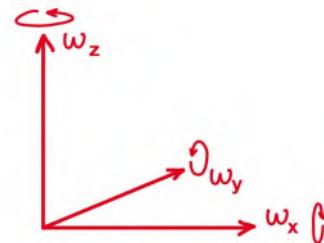
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3C Translation



Ground acceleration
Seismometer

+ 3C Rotation

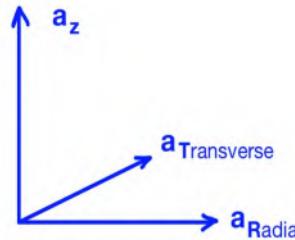


Rotation rate
Rotation sensor

$$\frac{a_T}{\dot{\omega}_z} = \frac{-k^2 c^2 A \sin(kx - kct)}{\frac{1}{2} k^2 c A \sin(kx - kct)} = -2c$$

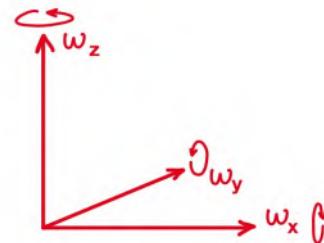
Combining Rotation and Translation

3C Translation



Ground acceleration
Seismometer

+ 3C Rotation



Rotation rate
Rotation sensor

$$\frac{\dot{a}_T}{\dot{\omega}_z} = \frac{-k^2 c^2 A \sin(kx - kct)}{\frac{1}{2} k^2 c A \sin(kx - kct)} = -2c$$

- + Rotation rate and acceleration should be **in phase**
- + amplitudes scaled by **two times the horizontal phase velocity.**

**phase velocity
in phase**

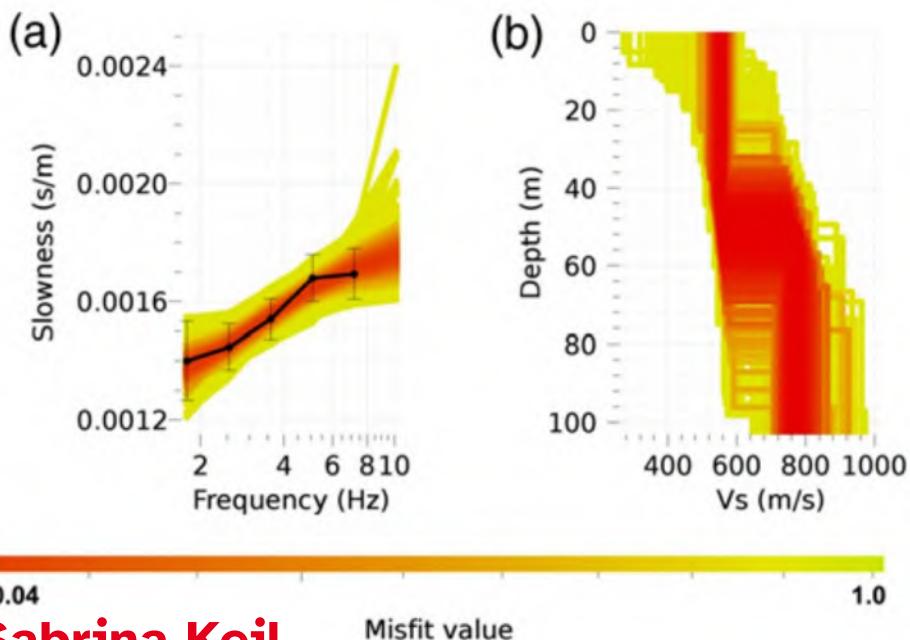
→ using single measurement of 6C
→ waveforms similar → can find source direction

→ **structure**
→ **source**

Structure – determining it using 6C

Single 6C-station dispersion curves:

$$c(f) = -\frac{1}{2} \ddot{u}_T(f) / \dot{\omega}_3(f)$$



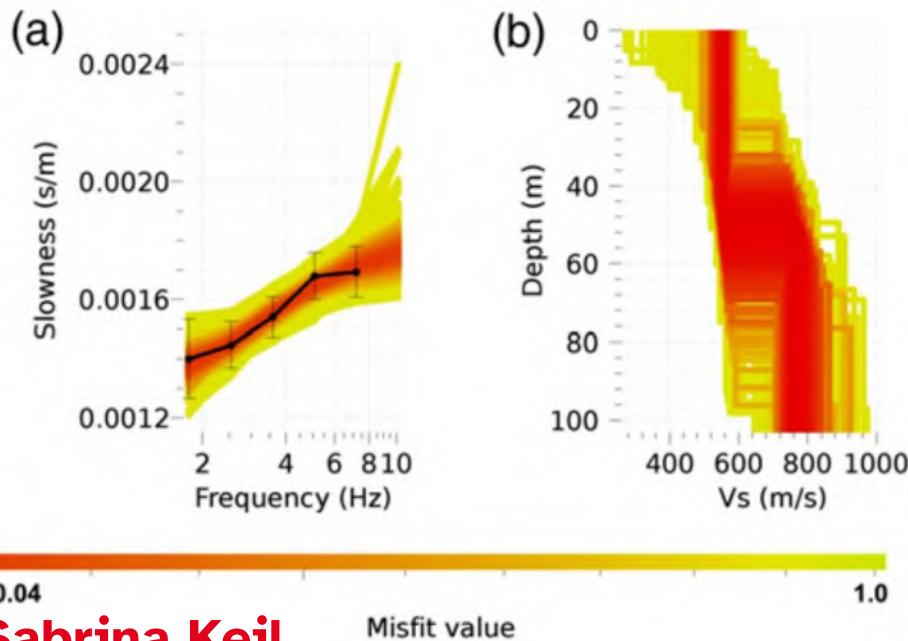
Sabrina Keil

Wassermann et al., BSSA 2016

Structure – determining it using 6C

Single 6C-station dispersion curves:

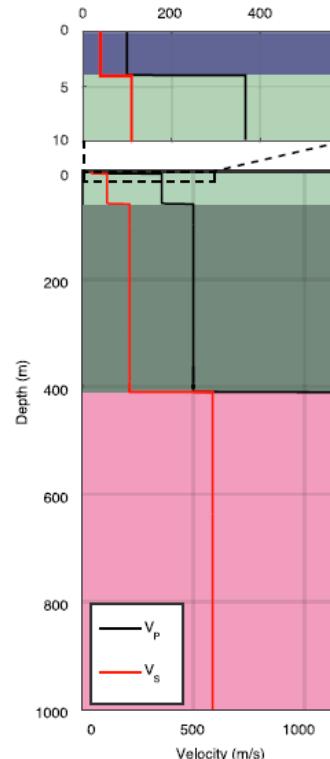
$$c(f) = -\frac{1}{2} \ddot{u}_T(f) / \dot{\omega}_3(f)$$



Sabrina Keil

Wassermann et al., BSSA 2016

Lunar V_p & V_s structure
“Point” 6C measurement



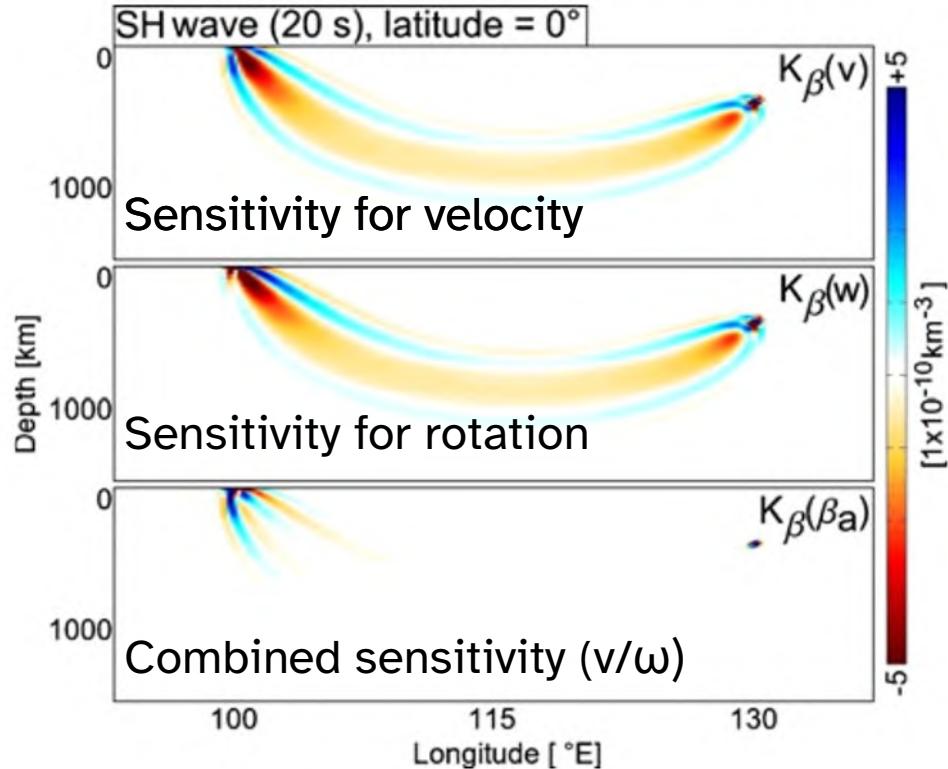
*Sollberger et al.,
GRL 2016*

Structure – sensitivity kernels

Sensitivity kernels for:

$$\frac{\dot{v}_T(x, t)}{\omega(x, t)} = -2c(x)$$

- + Local near surface structure
- + Without source info
- accurate amplitudes needed



Bernauer et al., Geophysics 2009
Fichtner & Igel, BSSA 2009
Bernauer et al., J. Seismol. 2012

Source

Structure

- Phase velocity
- Dispersion
- Sensitivity kernels

Instrumentation

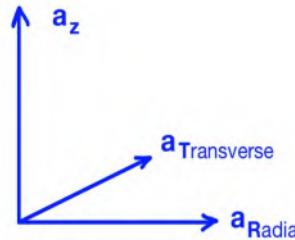
Wavefield

- Wavetype separation
- Wavetype ratios

Structural engineering

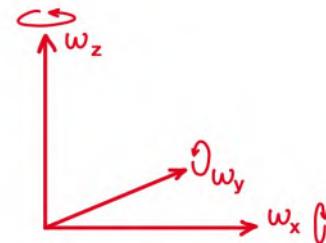
Combining Rotation and Translation

3C Translation



Ground acceleration
Seismometer

+ 3C Rotation



Rotation rate
Rotation sensor

$$\frac{\dot{a}_T}{\dot{\omega}_z} = \frac{-k^2 c^2 A \sin(kx - kct)}{\frac{1}{2} k^2 c A \sin(kx - kct)} = -2c$$

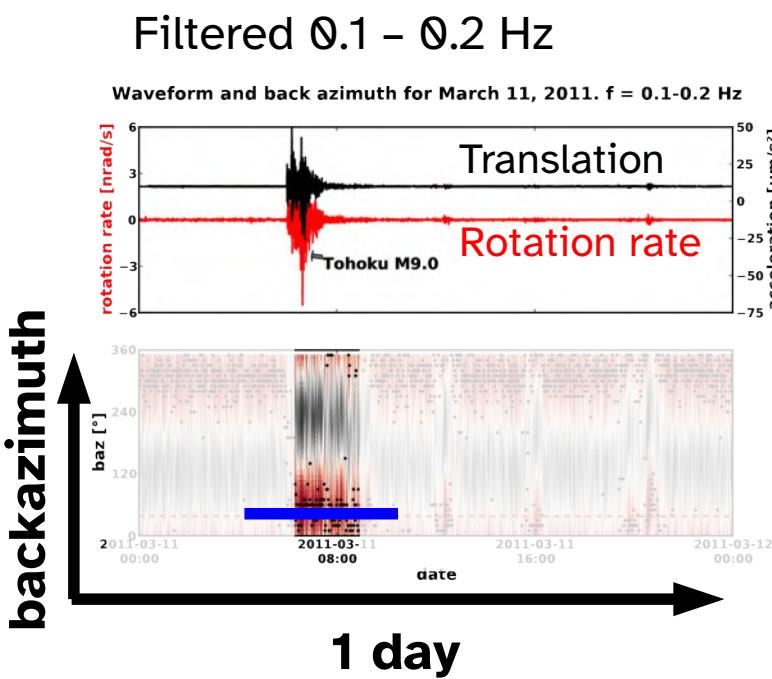
- + Rotation rate and acceleration should be **in phase**
- + amplitudes scaled by **two times the horizontal phase velocity.**

**phase velocity
in phase**

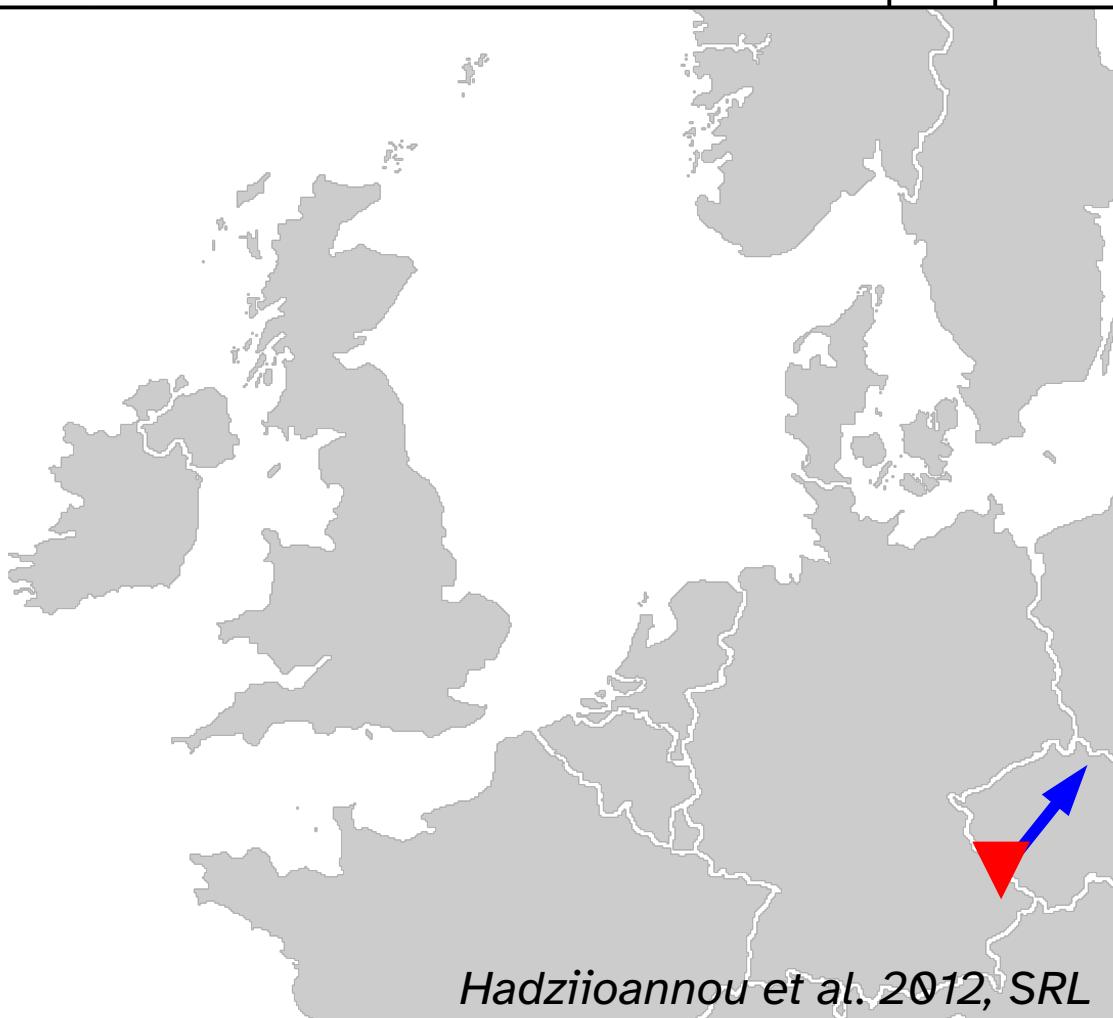
→ using single measurement of 6C
→ waveforms similar → can find source direction

→ **structure**
→ **source**

Source – source direction

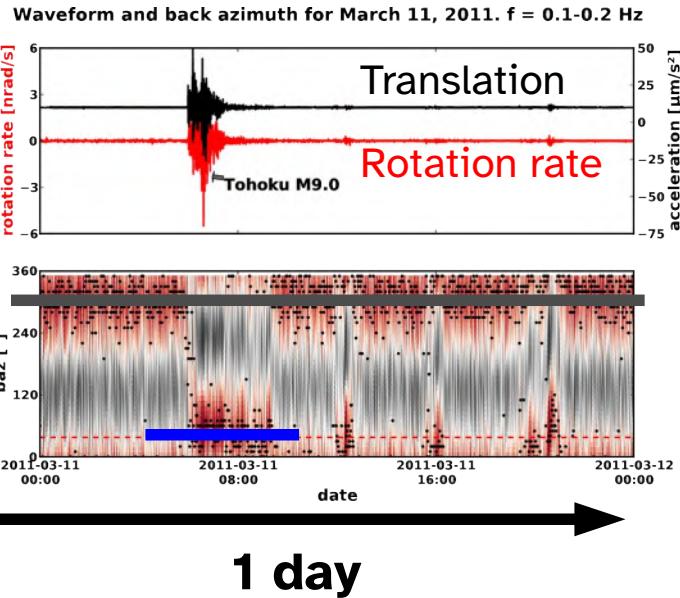


Corrcoef = 1
Corrcoef = -1

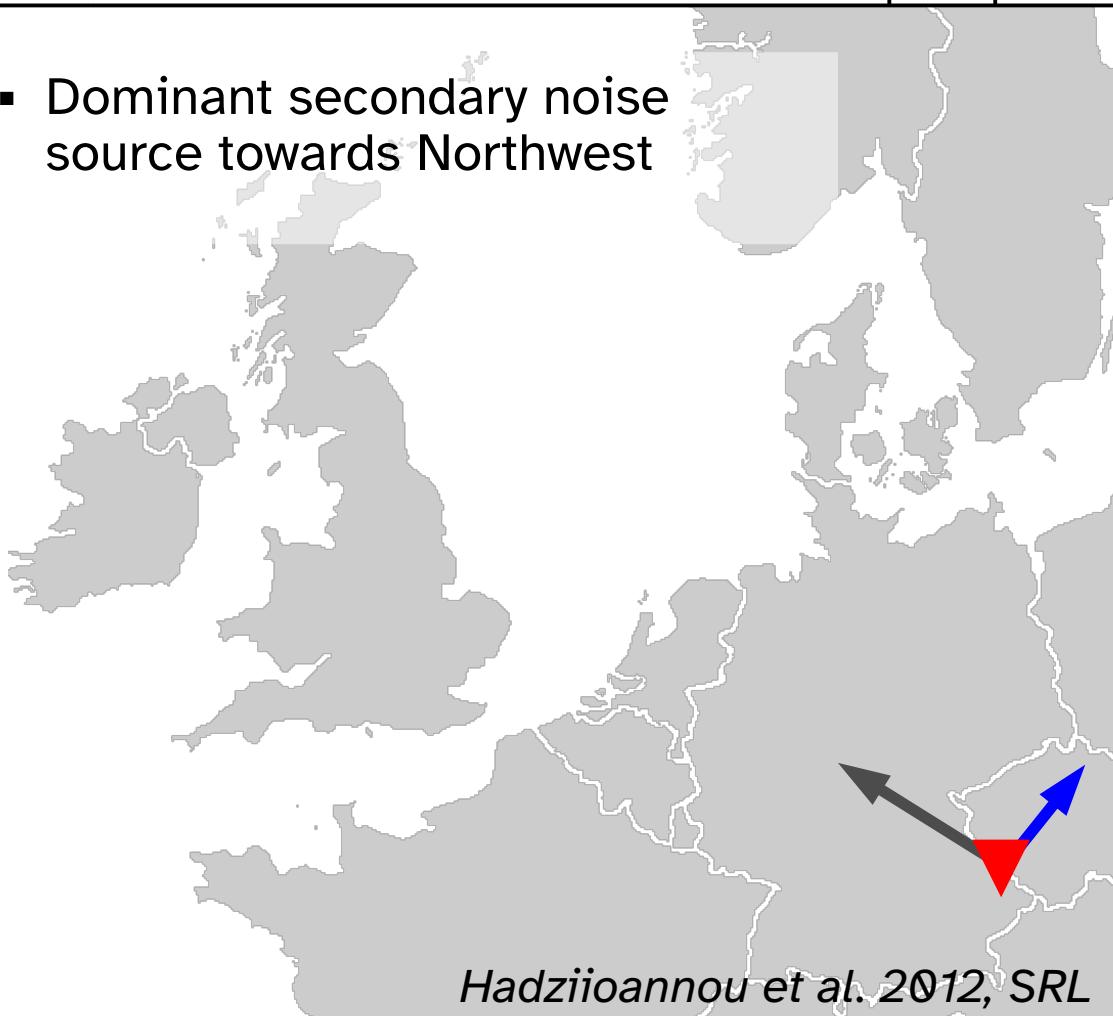


Source – source direction

Filtered 0.1 – 0.2 Hz



- Dominant secondary noise source towards Northwest



Source – source direction

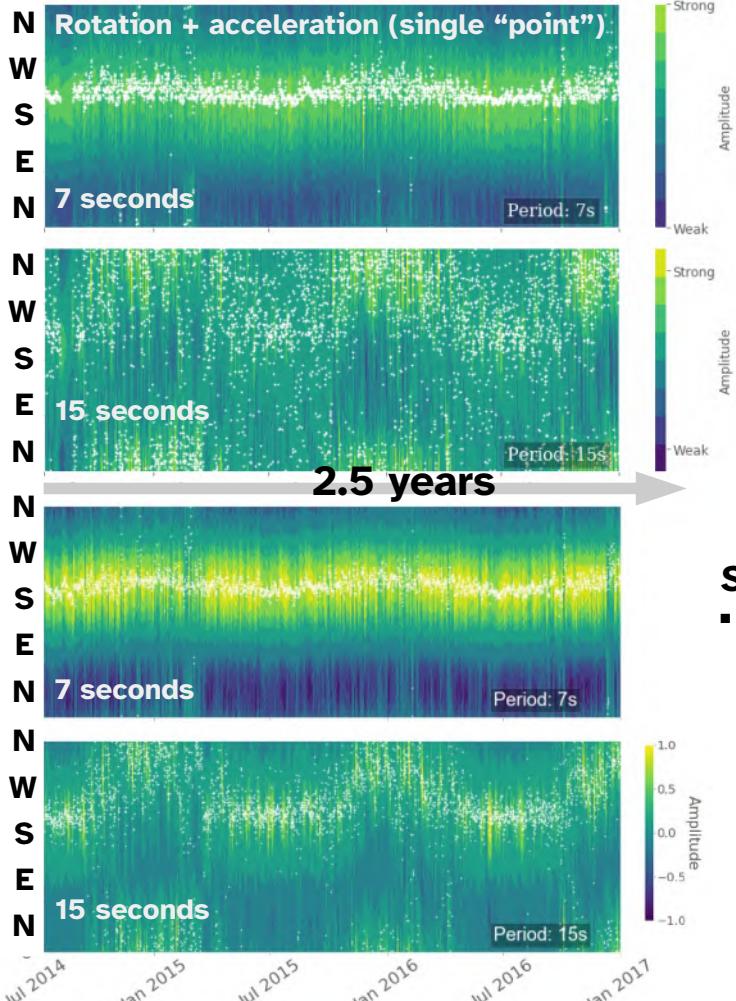


Single-point backazimuth determination

- Direction of secondary and primary microseism

Source – source direction

Love



Rayleigh



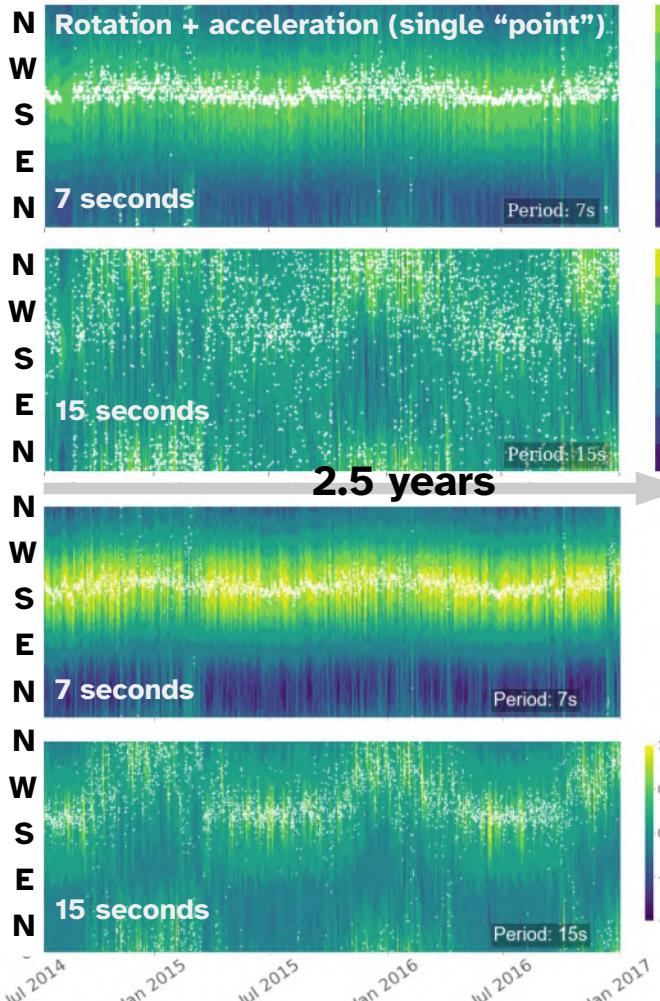
Single-point backazimuth determination

- Direction of secondary and primary microseism

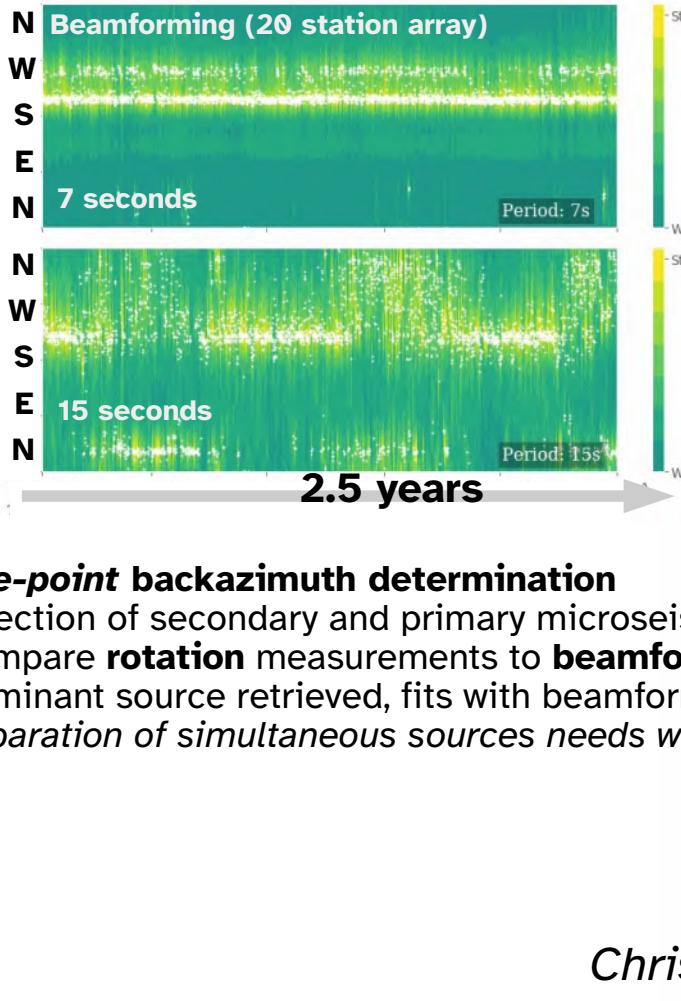


Source – source direction

Love



Rayleigh



Christoph Schroeer (UHH)

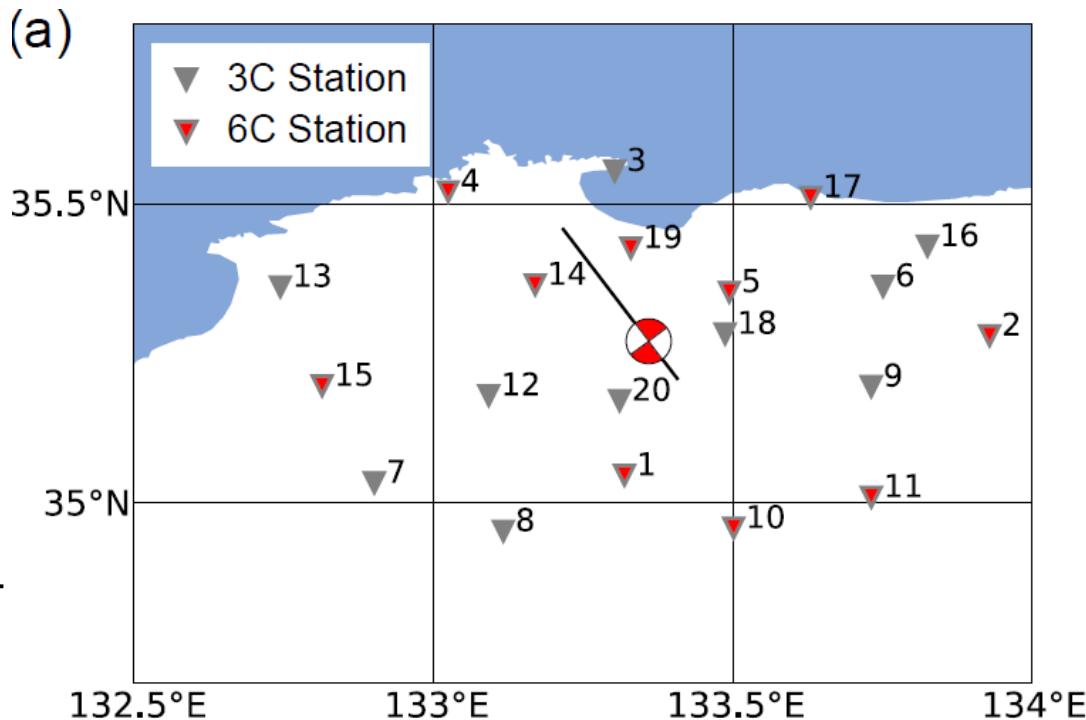


Single-point backazimuth determination

- Direction of secondary and primary microseism
- Compare **rotation** measurements to **beamforming**
- Dominant source retrieved, fits with beamforming
- *Separation of simultaneous sources needs work*

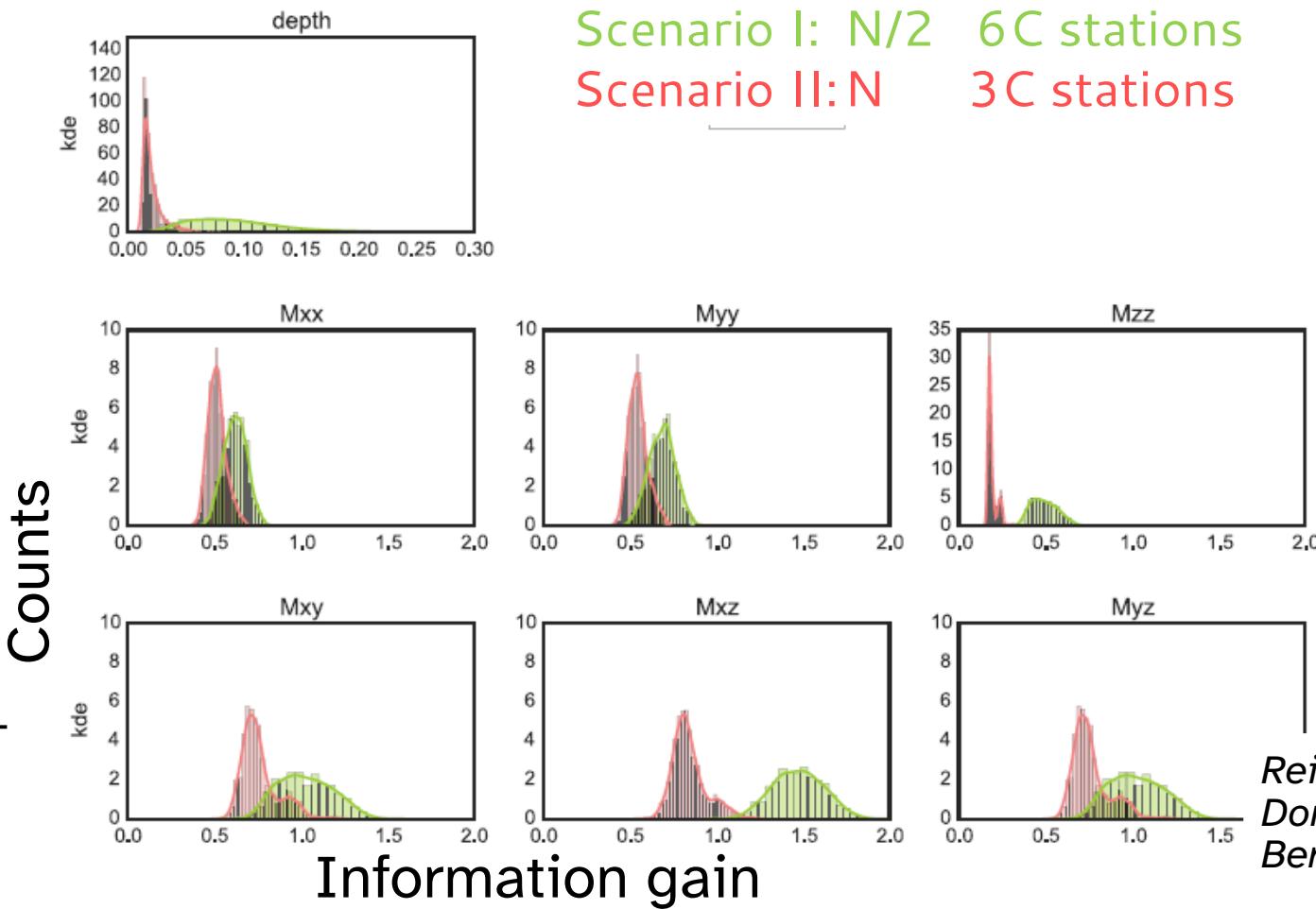
Earthquake Source inversion

improved constraints on kinematic and point source parameters with $\frac{1}{2}$ the stations
+ Scenario I: N receivers with 3C observations (translations)
+ Scenario II: N/2 receivers with 6C observations (translations and rotations)

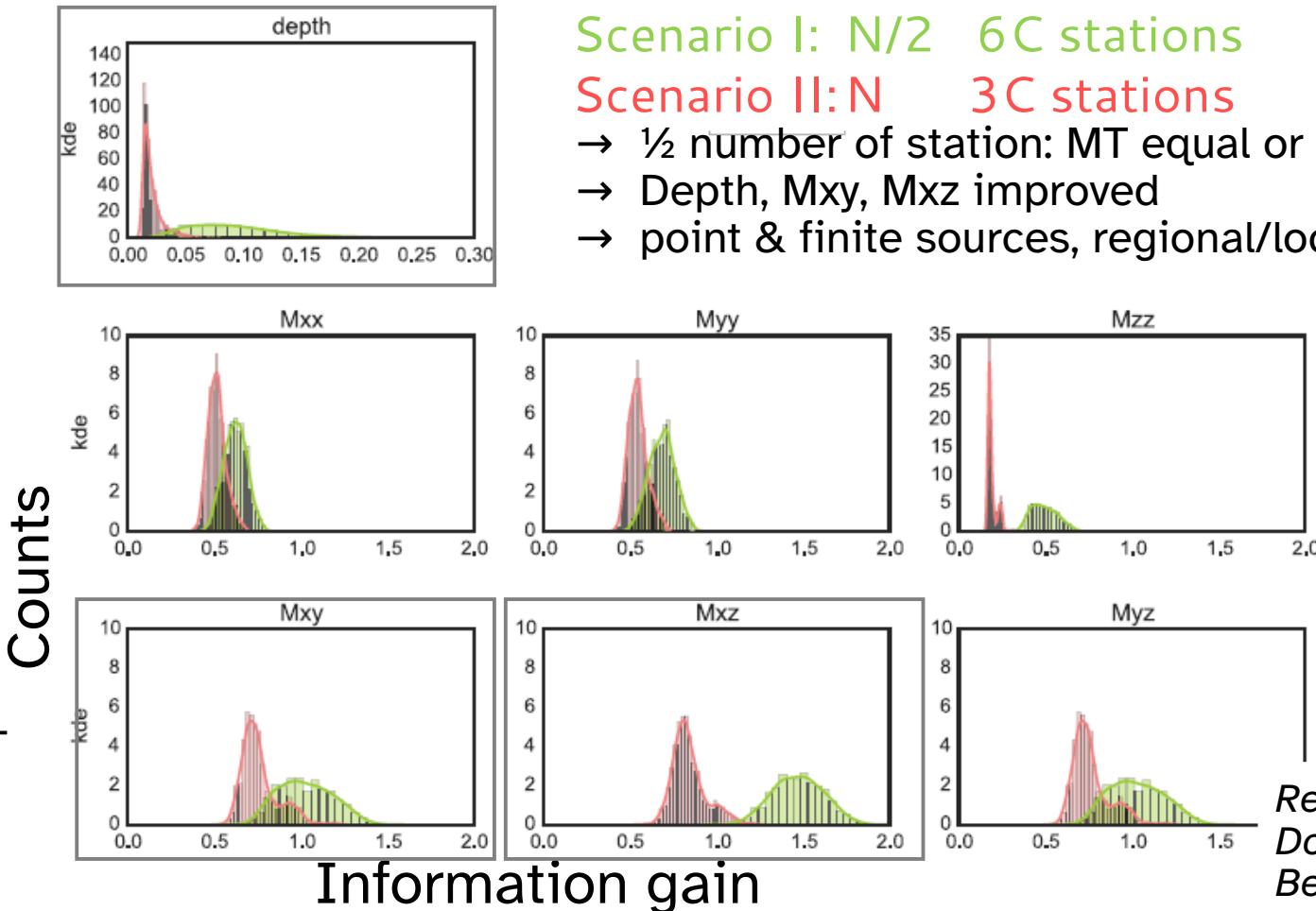


Reinwald et al., *Solid Earth* 2016
Donner et al., *GJI* 2016
Bernauer et al., *JGR: SE* 2014

Earthquake Source inversion



Earthquake Source inversion



Reinwald et al., *Solid Earth* 2016
Donner et al., *GJI* 2016
Bernauer et al., *JGR: SE* 2014

Source

- MT inversion
- Microseisms

Structure

- Phase velocity
- Dispersion
- Sensitivity kernels

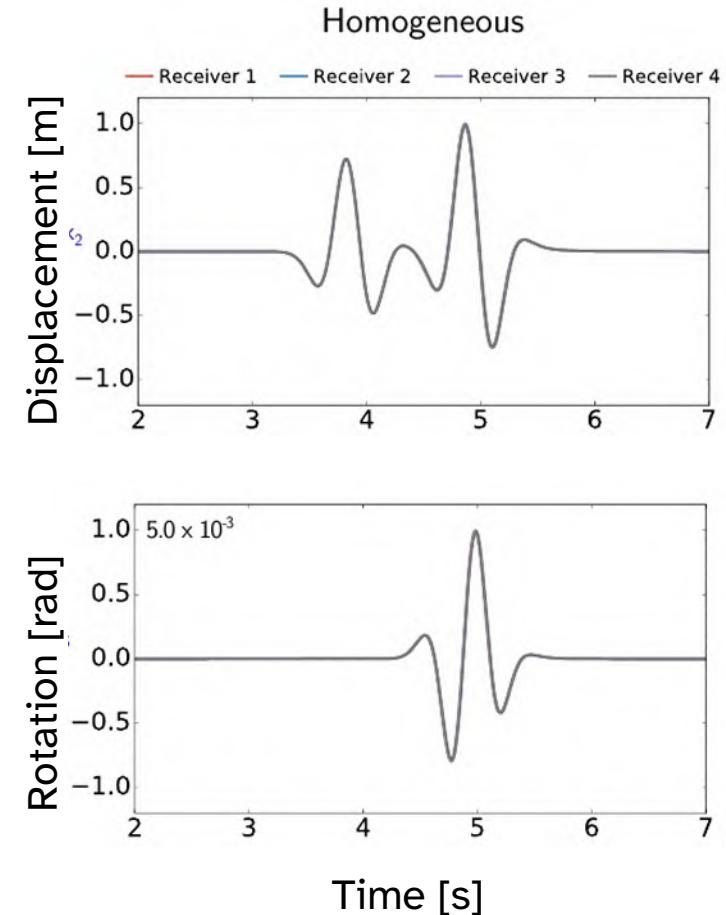
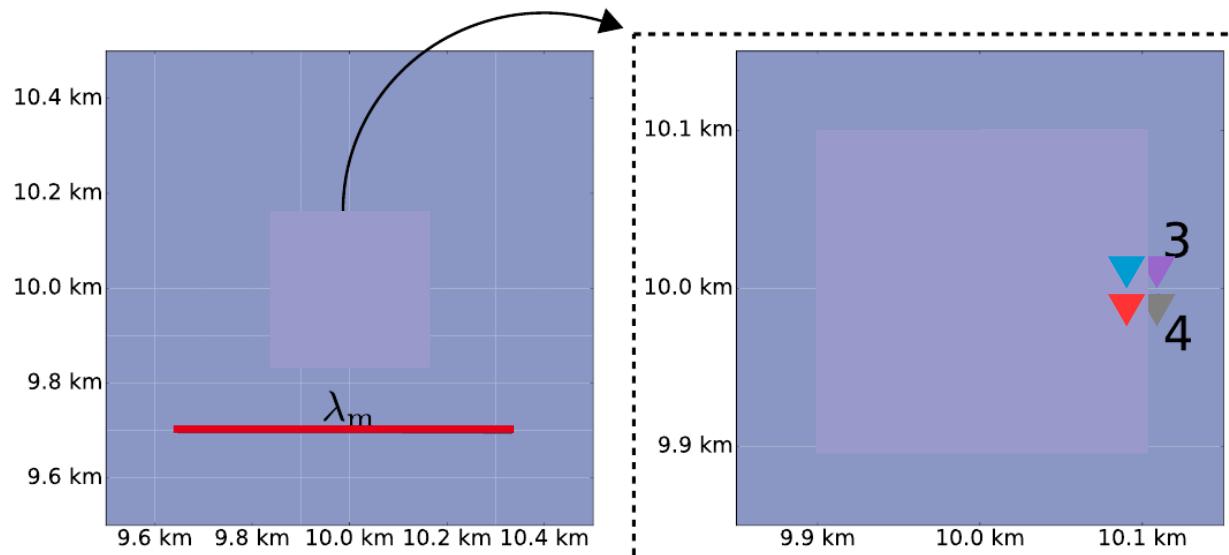
Instrumentation

Wavefield

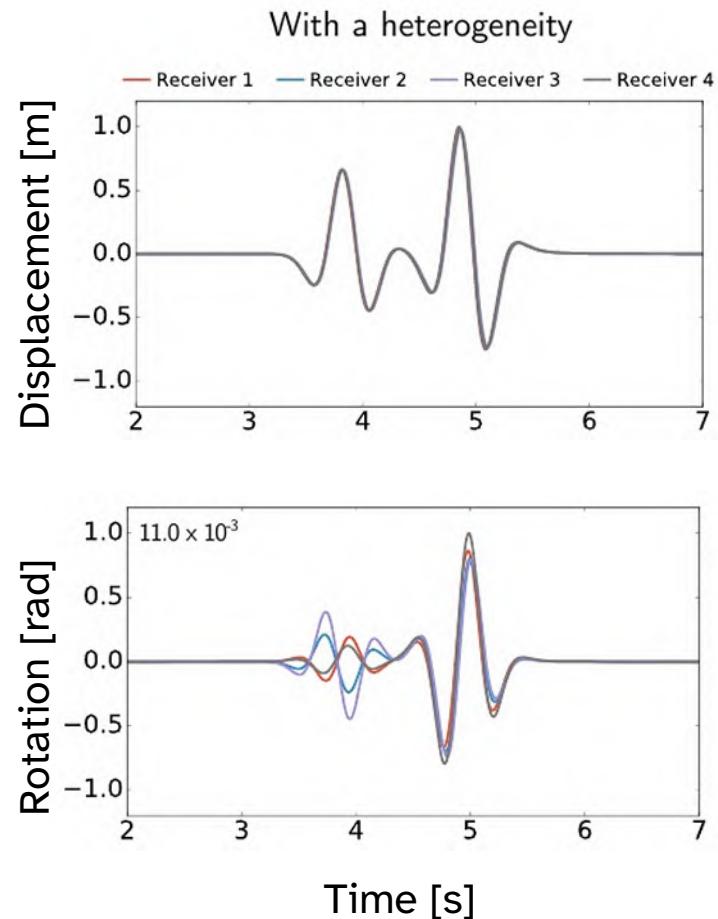
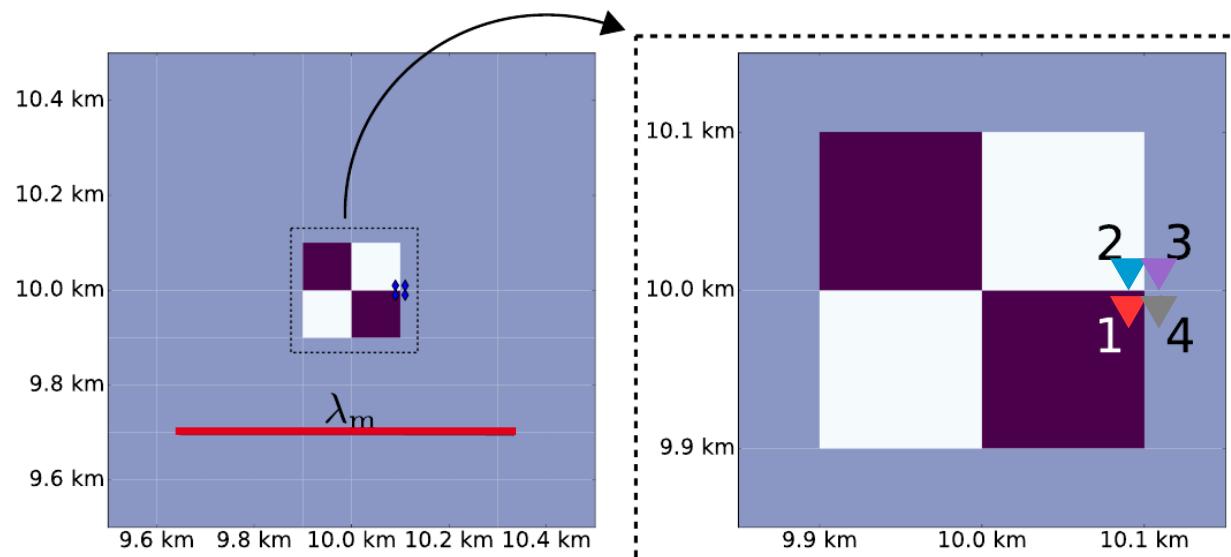
- Wavetype separation
- Wavetype ratios

Structural engineering

Structure – sensitivity to heterogeneity



Structure – sensitivity to heterogeneity



- displacement not sensitive to heterogeneity $1/3 \lambda$
- gradients (rotation, strain) are very sensitive!
- implications for e.g. tomography

Structure – civil engineering → structural health monitoring

Can we use *gradient measurements* to detect material changes? (Can we locate **damage**?)
Goal: more sensitive 6C measurements on buildings



Rotation + translation
sensors

increased load
 $300 \rightarrow 600 \rightarrow 900$ kg



Change pre-tension
of bridge

See Marco Dominguez Bureos' poster next week!
Chun-Man Liao et al., 2022

Source

- MT inversion
- Microseisms

Structure

- Phase velocity
- Dispersion
- Sensitivity kernels
- Heterogeneity

Instrumentation

Wavefield

- Wavetype separation
- Wavetype ratios

Structural engineering

- Structural changes
- Torsional modes
- Interstory drift

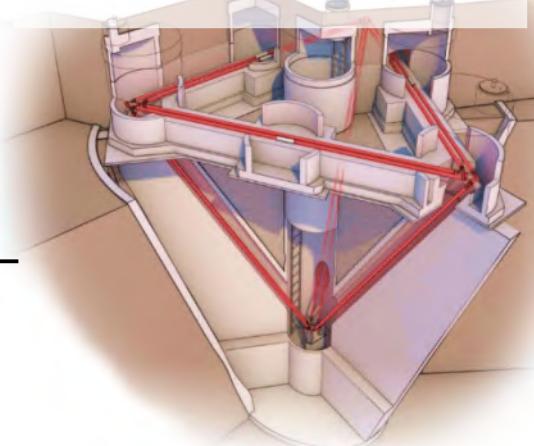
Instrumentation – How to observe rotations?

Observatory instruments

Ring lasers



Andreas Brotzer &
Felix Bernauer



Field instruments

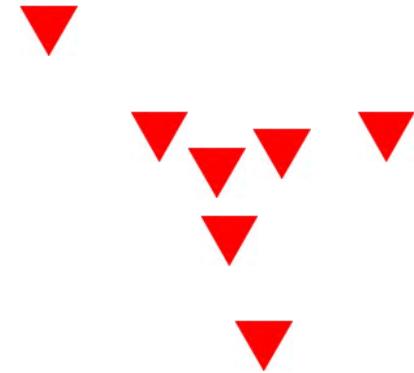
e.g. Fiber optic gyros



Laurent Mattio

Dense arrays

Seismometers



$$L < \frac{1}{4} \lambda$$

Instrumentation – Ring Lasers

Observatory instruments

Ring lasers

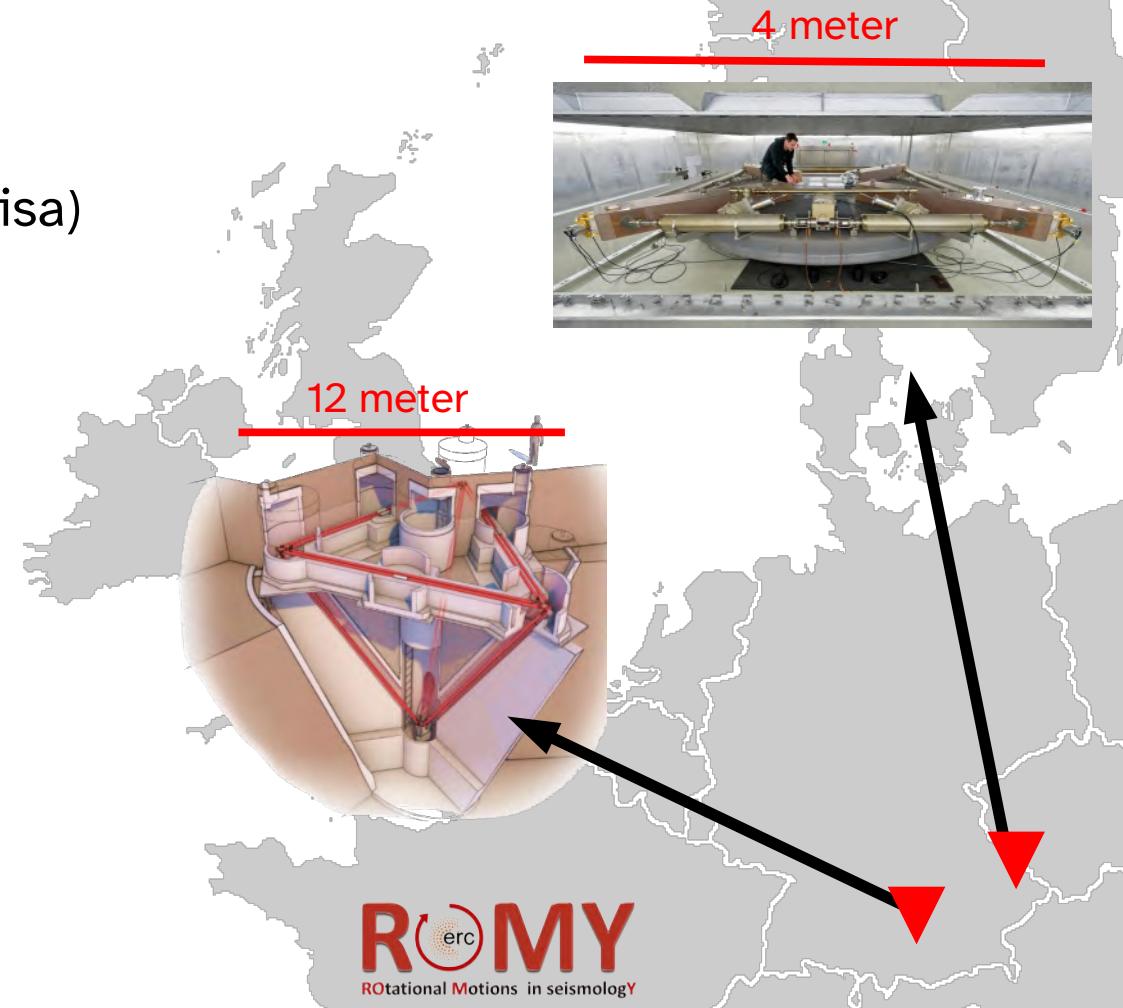
+ 6 worldwide (PFO, Christchurch, Pisa)

+ G-ring in Wettzell, Germany:

most sensitive

+ ROMY near Munich, Germany:

first 3-component rotation



“Lord of the Rings”, Science, 2017

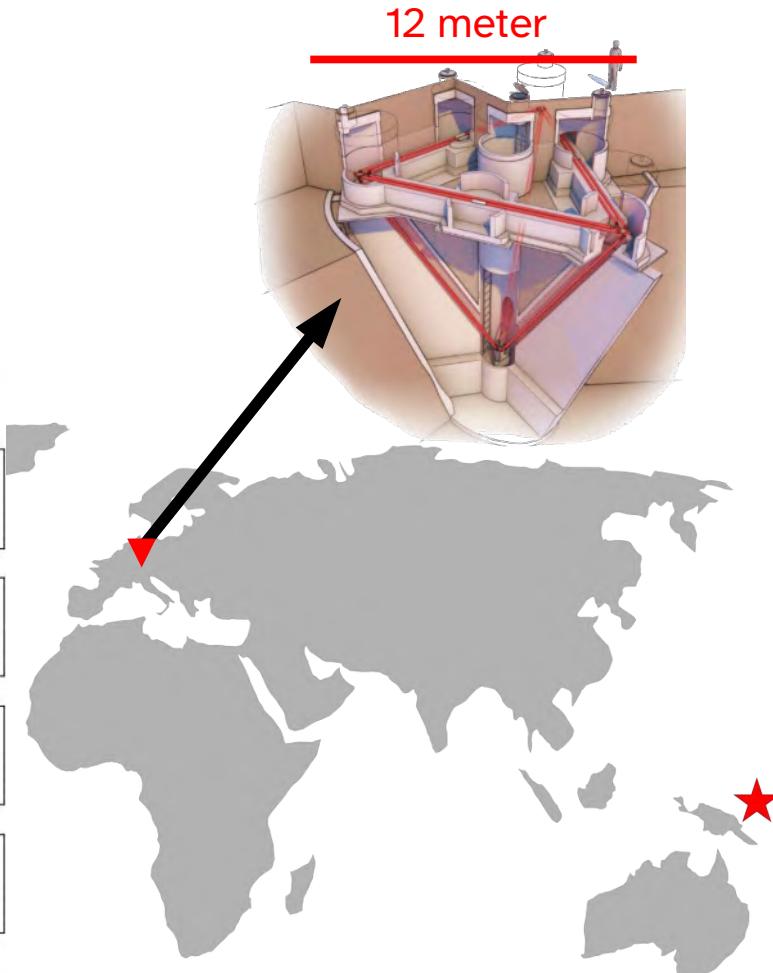
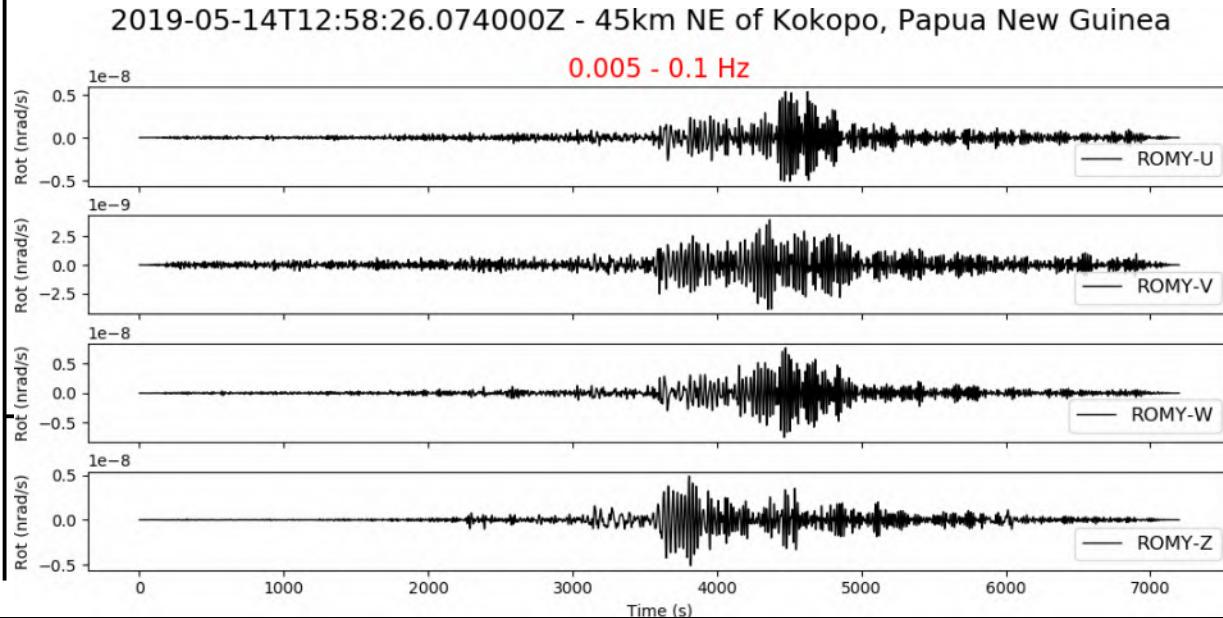
ROMY
ROTATIONAL MOTIONS in seismology

Instrumentation – Ring Lasers

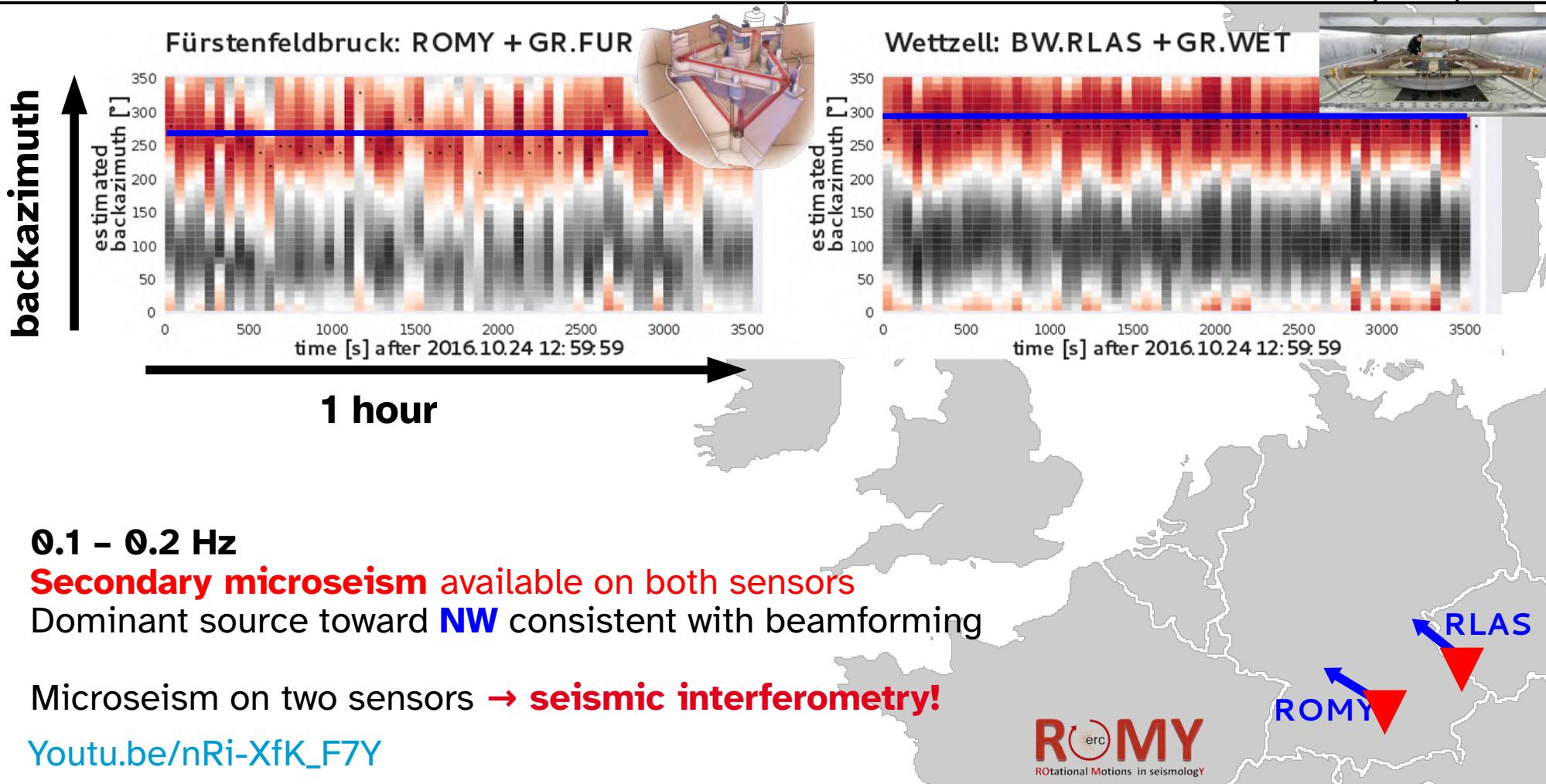
Observatory instruments

Ring lasers

- + ROMY: first 3-component rotation
- + first observation on all 4 rings:



Instrumentation – Ring Lasers



Source

- MT inversion
- Microseisms

Wavefield

- Wavetype separation
- Wavetype ratios

Instrumentation

- Observatory
- Field instruments
- Dense arrays

Structure

- Phase velocity
- Dispersion
- Sensitivity kernels
- Heterogeneity

Structural engineering

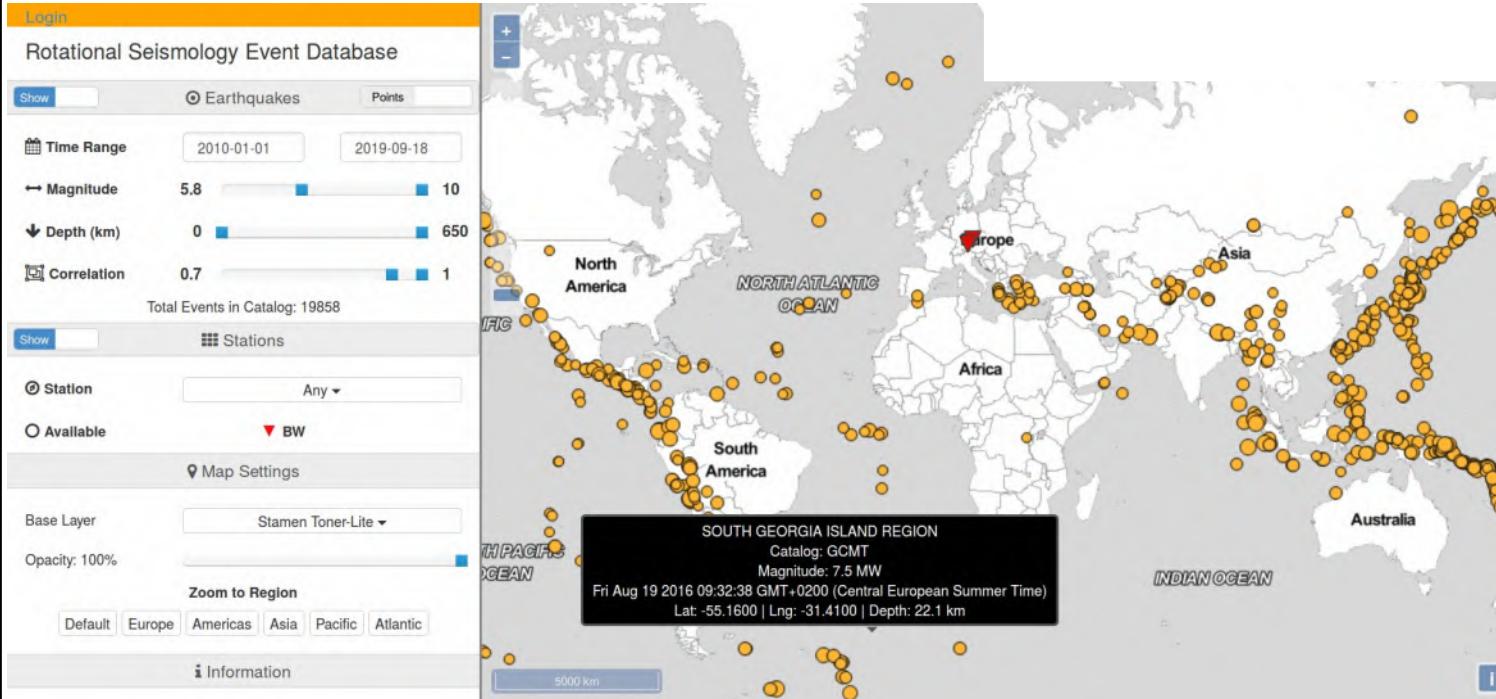
- Structural changes
- Torsional modes
- Interstory drift

Awesome, where do I start?

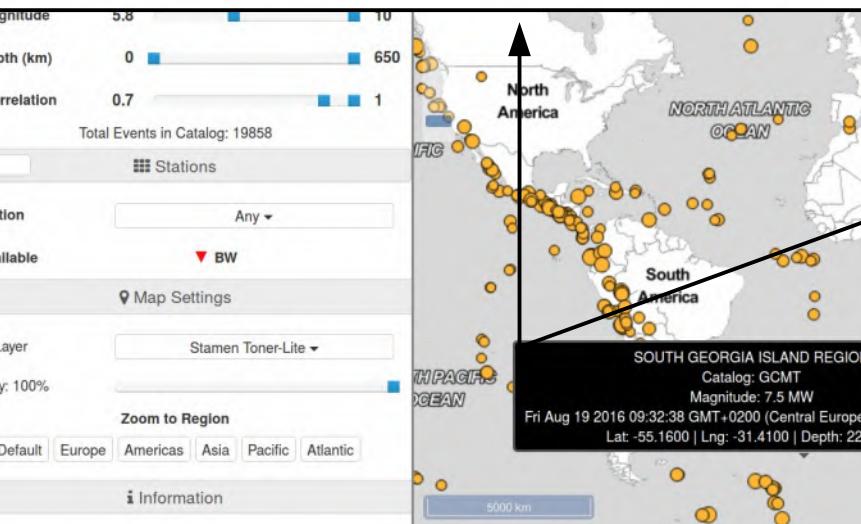
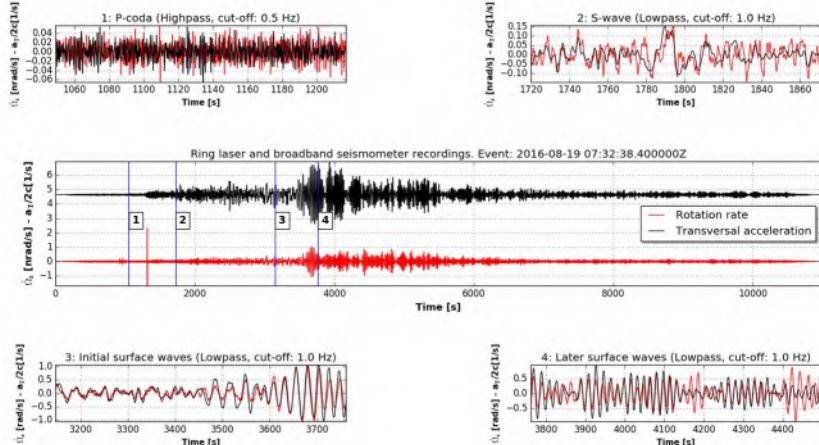
Rotational seismology database

Access via rotational-seismology.org → “Data”
Or rotations-database.geophysik.uni-muenchen.de

- Waveform download
- Example analysis
- Python code to start
- *Salvermoser et al., SRL 2017*

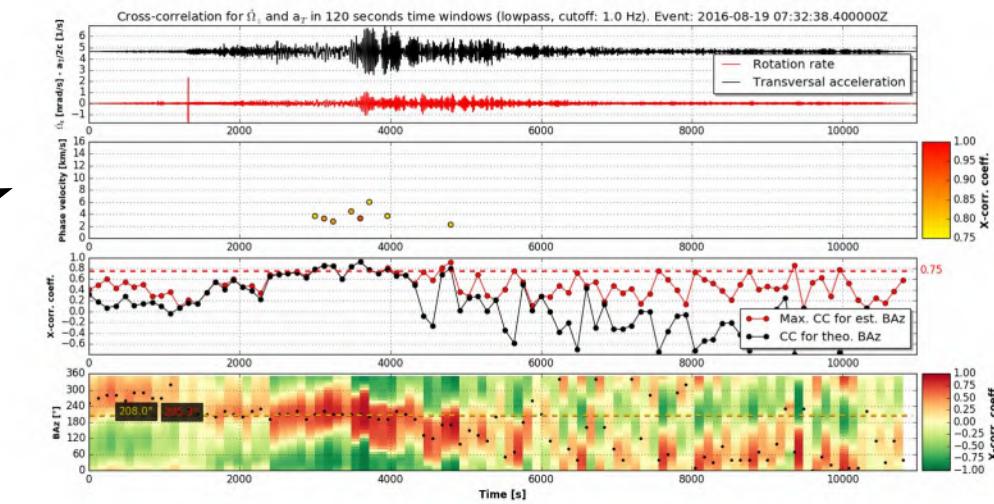


Rotational seismology database



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- **Example analysis**
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- *Salvermoser et al., SRL 2017*



How to get started



Activities • Chromium Web Browser • Mi Sep 18, 11:30 http://seismo-live.org/ - Chromium

http://seismo-live.org/ x download+preprocess... x + Not secure | seismo-live.org

tmpnb server: http://vm-141-40-254-17.cloud.mwn.de:8000

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Go to seismo-live.org
→ click green square to launch

How to get started

The screenshot shows a Linux desktop environment with two Chromium browser windows. The top window displays the seismo-live.org homepage, which features a sidebar with categories such as General Seismology, Glacial Seismology, Instaseis-Syngine, ObsPy, Python Introduction, Rotational Seismology, Downloading and Preprocessing, Backazimuth Estimation, Phase Velocity Estimation, Reproducible Papers, Seismic Inverse Problems, Signal Processing, and Workshops. Each category has a brief description and a 'VIEW ALL' button. The 'Rotational Seismology' section is expanded, showing three specific notebooks: 'Downloading and Preprocessing', 'Backazimuth Estimation', and 'Phase Velocity Estimation', each with an 'OPEN' button. The bottom window shows a similar list of notebooks for 'Rotational Seismology' with 'OPEN' buttons.

Go to seismo-live.org

→ click green square to launch
→ select “Rotational Seismology”

Notebooks for:

- Getting ringlaser data
- Backazimuth estimation
- Phase velocity estimation

How to get started

The image shows a Linux desktop environment with three windows open:

- A top-level Chromium browser window showing the seismo-live.org homepage.
- A terminal window below it displaying a Jupyter notebook interface with a Python 3 kernel.
- A third Chromium browser window showing a specific notebook titled "Rotational Seismology Tutorial: Data Download + Pre-Processing".

The notebook content includes:

- A title section: "Rotational Seismology Tutorial: Data Download + Pre-Processing".
- A bulleted list: "How do I download ring laser data?", "What pre-processing do I need to perform?", and "... and how can I do this using Obspy?".
- A code cell labeled "In [1]:" containing Python code for setting up matplotlib and plt.style.use('ggplot').
- A section titled "Pick events from catalog to define start- and endtimes of traces".
- A note explaining the purpose of picking an event from a catalog to compare waveform data of a ring laser and a collocated seismometer.

Go to seismo-live.org

→ click green square to launch
→ select “Rotational Seismology”
Notebooks for:

- Getting ringlaser data
 - Backazimuth estimation
 - Phase velocity estimation
- launch one of the notebooks
... and start playing with data!

.. a citation of Salvermoser et al., SRL 2017 is appreciated..

Source

- MT inversion
- Microseism

Wavefield

- Wavetype separation
- Scattering
- Wavetype ratios
- Tilt (OBS?)

Instrumentation

- Observatory
- Field instruments
- Dense arrays

Structure

- Phase velocity
- Dispersion
- Sensitivity kernels
- Heterogeneity
- Toroidal modes

Structural engineering

- Structural changes
- Torsional modes
- Interstory drift

Source

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- Torsional modes
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With 6C we have:

New observables

... to do more with fewer stations

... or with **single station!**

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- Access through www.romy-erc.eu → links

Get started with rotational data

- Seismo-live.org → rotational seismology → 3 introductory notebooks to reproduce some figures from the rotational database
- www.romy-erc.eu
- www.rotational-seismology.org (with mailing list!)